

Sometimes the chefs wanted to raise or lower the temperature by a large amount, but did not want to put the cubes into the cauldron one at a time. So for large jumps in temperature, they would put in or take out bunches of cubes.

For instance, if the chefs wanted to raise the temperature  $100^\circ$ , then they might toss five bunches of 20 hot cubes into the cauldron instead of 100 cubes one at a time. This saved a lot of time because they could have assistant chefs do the bunching.

When the chefs used bunches of cubes to change the temperature, they used a multiplication sign to record their activity. For example, to describe tossing five bunches of 20 hot cubes each into the cauldron, they would write  $+5 \bullet +20 = +100$  where,  $+5$  meant that five bunches were being added, and the  $+20$  showed that there were twenty hot cubes in each bunch.

The chefs could also change the temperature by removing bunches. For example, if they removed three bunches of 5 hot cubes each, the result was to lower the temperature  $15^\circ$ , because each time a bunch of 5 hot cubes was removed, the temperature went down 5 degrees. To record this change, they would write

$-3 \bullet +5 = -15$  where the  $-3$  meant that three bunches were being removed, and the  $+5$  showed that there were five hot cubes in each bunch.

- Each of the problems below describes an action by the chefs. Figure out how the temperature would change overall in each of these situations *and* write an equation to describe the action and the overall result.
  - Two bunches of 6 cold cubes each were added.
  - Four bunches of 7 hot cubes each were removed.
  - Three bunches of 6 cold cubes each were removed.
- Describe the action involving hot or cold cubes that is represented by each of the following arithmetic expressions and state how the temperature would change overall.
  - $-10 \bullet -5$
  - $+4 \bullet -8$

3. Model this expression:  $+4 \cdot -8$  using  $\square = 1$      $\blacksquare = -1$

Since multiplication is the same as repeated addition, how might we show the multiplication of integers using a number line?

4. Show how to do the following problem using a number line.

$$+3 \cdot -2$$



5. Write rules that might be used to multiply integers.
6. How could these same rules be used to divide integers? Why?
7. Use a different model to demonstrate each of the following:
- a.  $3 \times (-5)$                       b.  $(-3) \times 5$                       c.  $(-3) \times (-5)$